

HIGH RESOLUTION VACUUM ULTRA-VIOLET EMISSION SPECTRA OF ATOMIC IONS

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PNPS Workshop "Laboratory Astrophysics",
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Outline

- Introduction
- Experimental and theoretical methods
- Examples of results
- Summary

Laboratory works carried on in the Meudon Observatory

Jean-François Wyart, Lab. Aimé Cotton, Orsay, associated to the Paris-Meudon Observatory

Collaborations

- Ali Meftah (ass. Observatory), Djamel Deghiche and colleagues, PhD students, University Mouloud Mammeri in Tizi-Ouzou, Algeria

Nd IV, Nd V, Tm IV (Phys. Scr. 2007-2008)

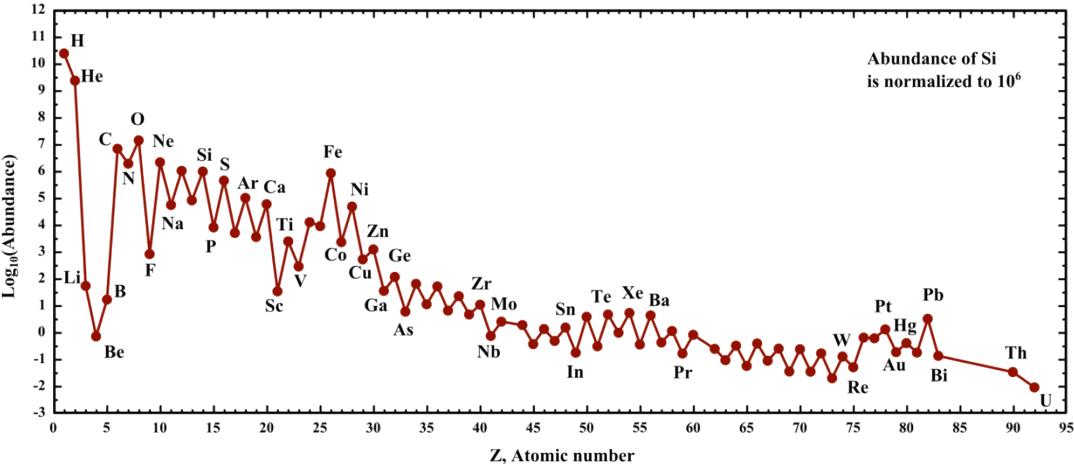
Recently Yb V (PS 2013), Nd V (core-excited config.) (PS 2015) and Er IV (JPB 2016).

- Alexander Rybtsev and colleagues Institute of Spectroscopy Troitsk, Moscow, Russia (IAEA-CRP 2010-2014)

W VIII (2013) and isoelectronic ions of Hf VI (2013), TaVII (2014), Re IX(2015), W IX (ATOMS 2015)

Technical support in the Meudon Observatory

- Norbert Champion, Christophe Blaess



Transition metals and other heavy elements : Lanthanides, actinides

PERIODIC TABLE
Atomic Properties of the Elements

NIST
National Institute of Standards and Technology
U.S. Department of Commerce

		Periodic Table of the Elements																																																																			
Group	Element	1		2		3		4		5		6		7		8		9		10		11		12		13		14		15		16		17		18																																	
		IA	IB	IIA	IIIA	IVA	VIA	VA	IB	VB	VIIB	VIIIB	VIIB	VIIIB	VIIB	VIIIB	VIIB	VIIIB	VIIIB	VIIB	VIIIB	VIIB	VIIIB	VIIB	VIIIB	VIIB	VIIIB	VIIB	VIIIB	VIIB	VIIIB	VIIB	VIIIB	VIIB	VIIIB																																		
1	H	$^1S_{1/2}$		Li	$^1S_{1/2}$				Be			Sc			Ti			Zr			Nb			In			Pr			Pt			Th			U																																	
2																																																																					
3																																																																					
4	K	$^{1S_{1/2}}$		Ca	$^{1S_{1/2}}$				Sc	$^{2D_{3/2}}$			Ti	$^{3F_{3/2}}$		V	$^{3F_{3/2}}$		Mn	$^{5S_{1/2}}$		Fe	$^{6D_{5/2}}$		Co	$^{7F_{5/2}}$		Ni	$^{7S_{1/2}}$		Cu	$^{10D_{7/2}}$		Zn	$^{13P_{3/2}}$		Ga	$^{13P_{3/2}}$		Ge	$^{14P_{3/2}}$		As	$^{15P_{3/2}}$		Pd	$^{15P_{3/2}}$		Al	$^{15P_{3/2}}$		Si	$^{15P_{3/2}}$		S	$^{16P_{3/2}}$		Cl	$^{17P_{3/2}}$		Ar	$^{18P_{3/2}}$							
5	Rb	$^{1S_{1/2}}$		Sr	$^{2D_{3/2}}$				Y	$^{3D_{1/2}}$			Zr	$^{3F_{5/2}}$		Sc	$^{4F_{3/2}}$		Tc	$^{5S_{1/2}}$		Mn	$^{6D_{5/2}}$		Fe	$^{7F_{5/2}}$		Co	$^{7S_{1/2}}$		Ni	$^{10D_{7/2}}$		Cu	$^{13P_{3/2}}$		Zn	$^{13P_{3/2}}$		Ga	$^{13P_{3/2}}$		Ge	$^{14P_{3/2}}$		As	$^{15P_{3/2}}$		Pd	$^{15P_{3/2}}$		Al	$^{15P_{3/2}}$		Si	$^{15P_{3/2}}$		S	$^{16P_{3/2}}$		Cl	$^{17P_{3/2}}$		Ar	$^{18P_{3/2}}$				
6	Cs	$^{1S_{1/2}}$							Yttrium	$^{3D_{1/2}}$			Zr	$^{3F_{5/2}}$		Titanium	$^{3F_{3/2}}$		Vanadium	$^{3F_{3/2}}$		Chromium	$^{4S_{1/2}}$		Manganese	$^{5D_{3/2}}$		Iron	$^{6F_{5/2}}$		Cobalt	$^{7S_{1/2}}$		Nickel	$^{10D_{7/2}}$		Copper	$^{13P_{3/2}}$		Zn	$^{13P_{3/2}}$		Ga	$^{13P_{3/2}}$		Ge	$^{14P_{3/2}}$		As	$^{15P_{3/2}}$		Pd	$^{15P_{3/2}}$		Al	$^{15P_{3/2}}$		Si	$^{15P_{3/2}}$		S	$^{16P_{3/2}}$		Cl	$^{17P_{3/2}}$		Ar	$^{18P_{3/2}}$	
7	Fr	$^{1S_{1/2}}$		Ra	$^{2D_{3/2}}$																																																																
8																																																																					

Complex spectra

$d^N, d^{N-1}nl, f^N, f^{N-1}nl$

Atomic Number
Ground-State Level
Symbol
Name
Standard Atomic Weight^a
Ground-State Configuration

Lanthanides
Actinides

58 **Ce** $^{1G_{9/2}}$
Lanthanum (139.0547) $[Xe]4f^1$
5.5386
5.5769

58 **Ce** $^{1G_{9/2}}$
Curium (140.116) $[Xe]4f^1$
5.5386
5.4753

59 **Pr** $^{1I_{15/2}}$
Praseodymium (140.907) $[Xe]4f^3$
5.6209
5.4975

60 **Eu** $^{1I_{15/2}}$
Promethium (144.242) $[Xe]4f^5$
5.6209
5.5822

61 **Sm** $^{1H_{11/2}}$
Samarium (150.36) $[Xe]4f^6$
5.6437
5.5838

62 **Gd** $^{1D_{15/2}}$
Gadolinium (151.964) $[Xe]4f^7$
5.6704
5.5931

63 **Eu** $^{1D_{15/2}}$
Europium (158.9235) $[Xe]4f^7$
5.6704
5.6838

64 **Gd** $^{1G_{9/2}}$
Dysprosium (162.500) $[Xe]4f^9$
5.6704
5.5931

65 **Tb** $^{1I_{11/2}}$
Terbium (164.93033) $[Xe]4f^9$
5.6704
5.6838

66 **Dy** $^{1I_{11/2}}$
Dysprosium (167.259) $[Xe]4f^10$
5.6704
5.6838

67 **Ho** $^{1G_{9/2}}$
Holmium (168.33422) $[Xe]4f^10$
5.6704
5.6838

68 **Tm** $^{1G_{9/2}}$
Thulium (172.054) $[Xe]4f^10$
5.6704
5.6838

69 **Er** $^{1G_{9/2}}$
Erbium (173.054) $[Xe]4f^10$
5.6704
5.6838

70 **Yb** $^{1D_{15/2}}$
Ytterbium (174.966) $[Xe]4f^10$
5.6704
5.6838

71 **Lu** $^{1D_{15/2}}$
Lutetium (175.066) $[Xe]4f^10$
5.6704
5.6838

^aBased upon ^{12}C . () indicates the mass number of the longest-lived isotope.

IUPAC conventional atomic weights; standard atomic weights for these elements are expressed in intervals; see iupac.org for an explanation and values.

For a description of the data, visit physics.nist.gov/data

Motivations

Useful data for interpretation of NLET line formation :

λ , gA , energy levels, SHF, IS, Landé factors, collision rates
⇒ Collisional-radiatif model of plasmas

Astrophysical plasmas

Interpretation of observed VUV spectra :

HST, FUSE, SOHO. Futures missions : WSO, ARAGO, LUVOIR

Chemically peculiar stars : elemental abundances

White Dwarfs : variation of fundamental constants (Berengut, Flambaum, Webb)

Large contribution to opacities

Ex : Lanthanides and actinides ions predicted to be present in emission of neutron stars mergers (Kasen, Badnell & Barnes)

Solar Physics

Magnetic-field-induced transitions (MIT) for diagnostic of magnetic field

Laboratory plasmas

Fusion applications : Tungsten ions

Triply charged Lanthanides:

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Solid state laser material, lighting industry, films etc

Spectra of moderately charged ions

Production of high resolution laboratory spectra
(fine or hyperfine structures)

+

Analysis of complex spectra based on :

- Ritz combination principle $\sigma = E_{\text{sup}} - E_{\text{inf}}$
- Theoretical and semi-empirical calculations of level structure



Linelist with λ , relative intensities and identifications

+

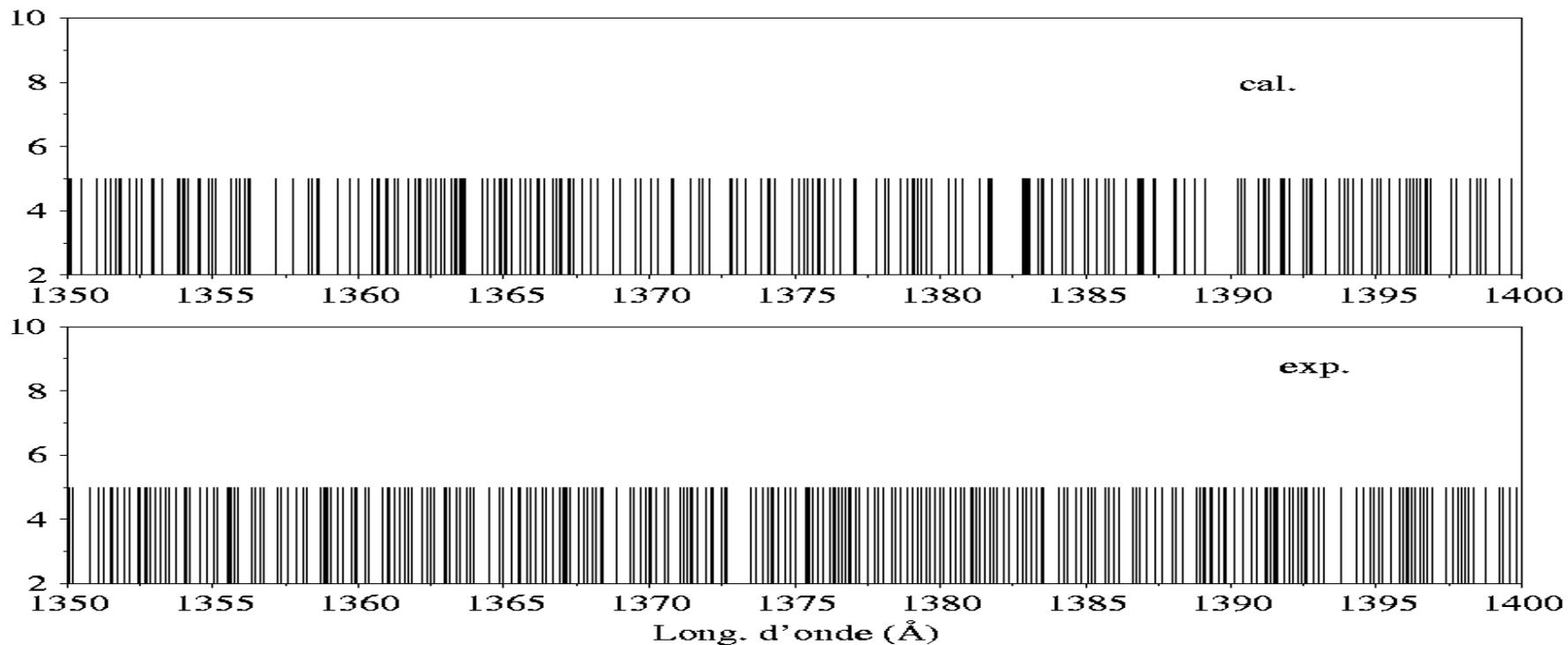
Level energies and wavefunctions in intermediate coupling scheme

+

gA , lifetimes, branching ratios, Landé factors

The Nd IV spectrum

Direct identification between λ_{cal} and λ_{exp} : impossible



10 m high resolution VUV spectrograph

Meudon Observatory



- Concave holographic grating 3600 lines/mm dispersion = $0.25 \text{ \AA} / \text{mm}$ first order.
- Resolution $\sim 150\,000$ (8m\AA , slit $30\mu\text{m}$)
- Wavelength range : $200\text{-}3000 \text{ \AA}$
- One single exposure : $\sim 2 \times 120 \text{ \AA}$ on two photographic plates or image plates

Light sources : high voltage vacuum sparks and hollow cathode for **atomic ion spectra** with fine (or HF) structures ;

Penning discharge in molecular gas for **electronic transitions of molecules** with rotational resolution

Erbium spark spectrum

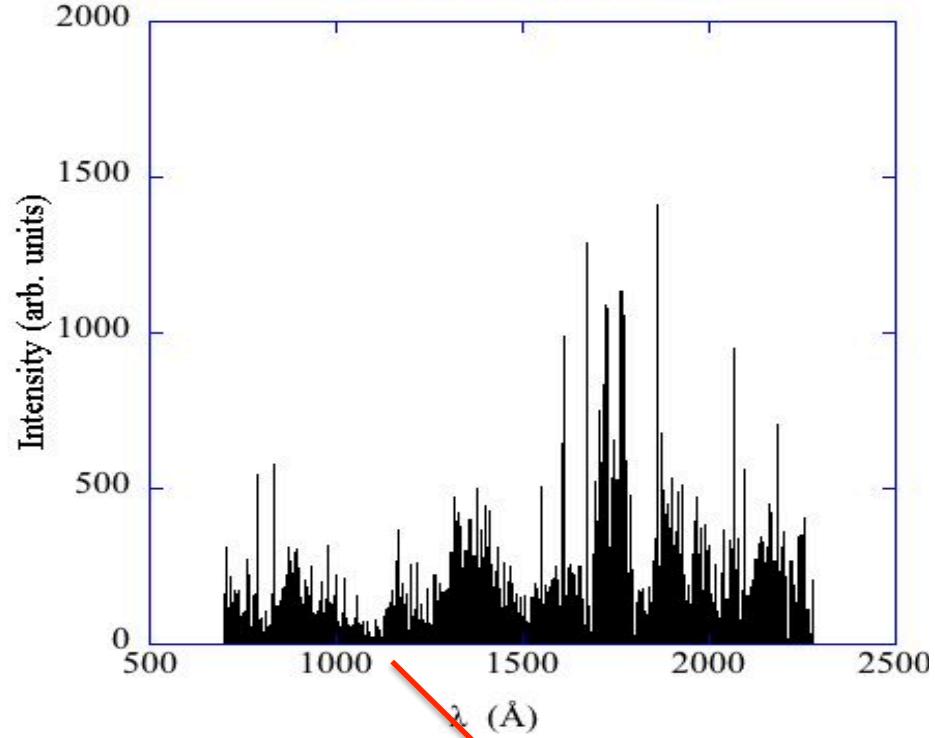
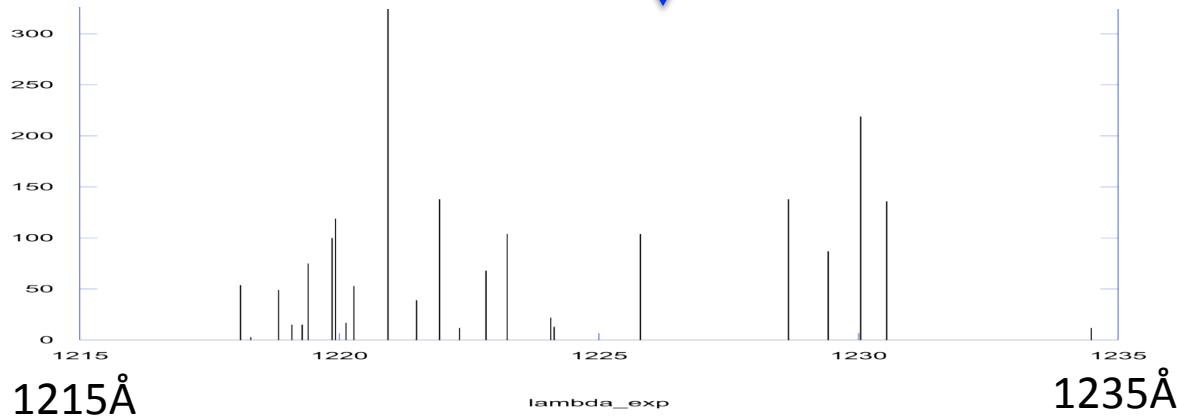


Image plate

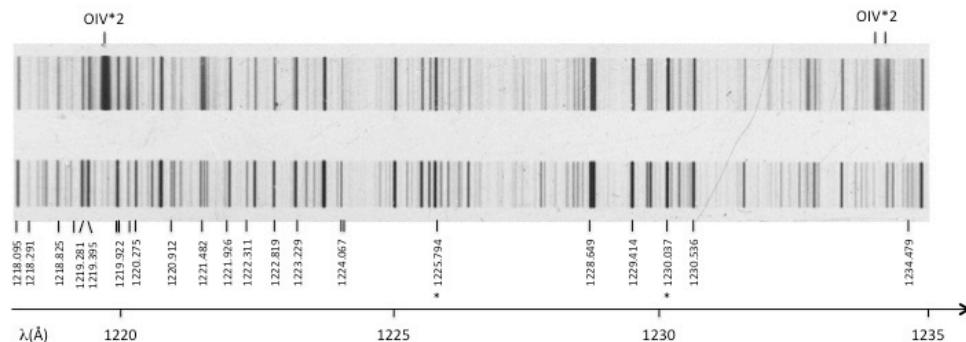
linear intensity response
over 5 orders of magnitude



Emission light sources :
vacuum spark source

Photographic plate

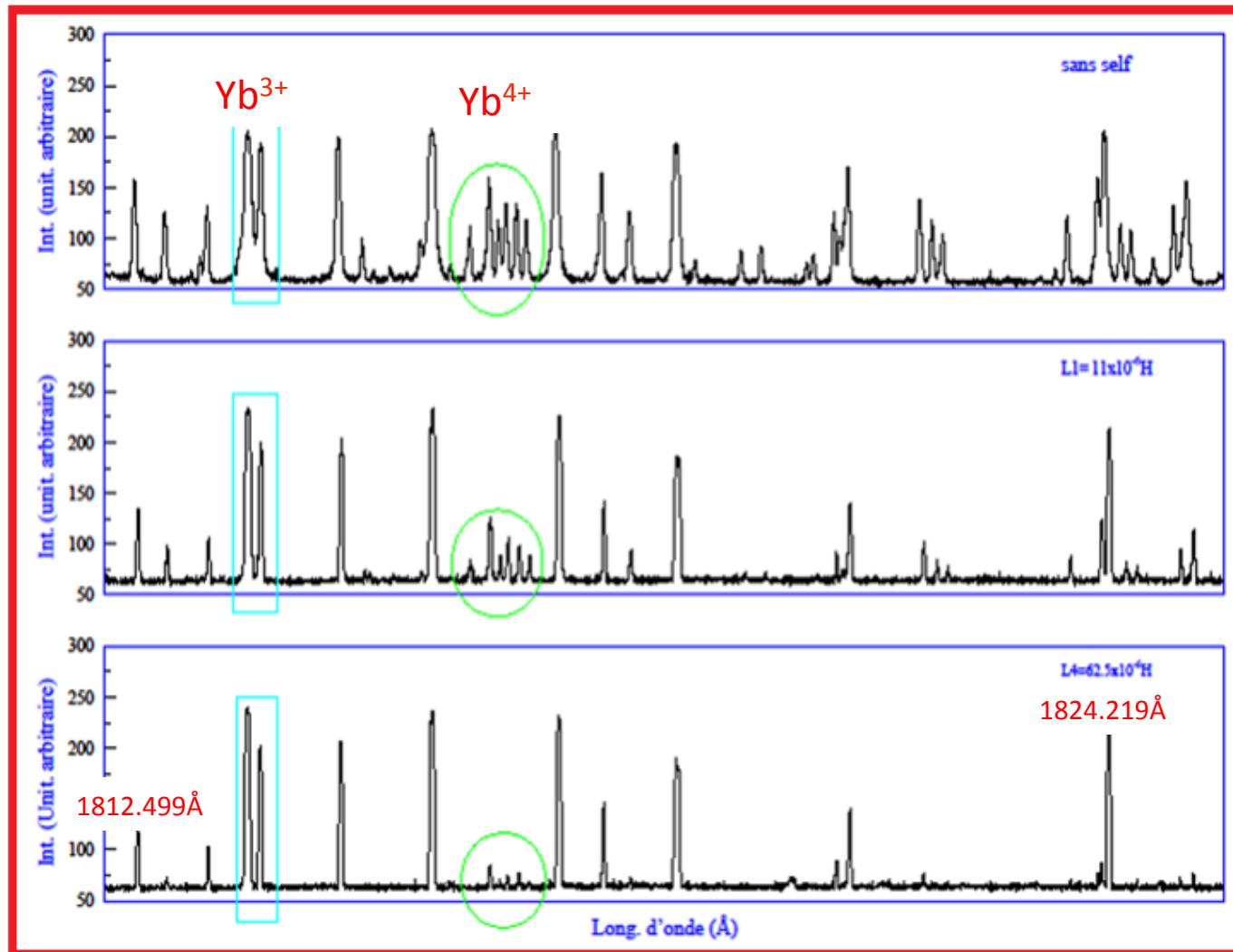
Calibration with references :
 $\Delta\lambda = \pm 0.001\text{--}0.005\text{\AA}$



Differentiation of ionization stages

Ytterbium vacuum spark spectrum

Inductance



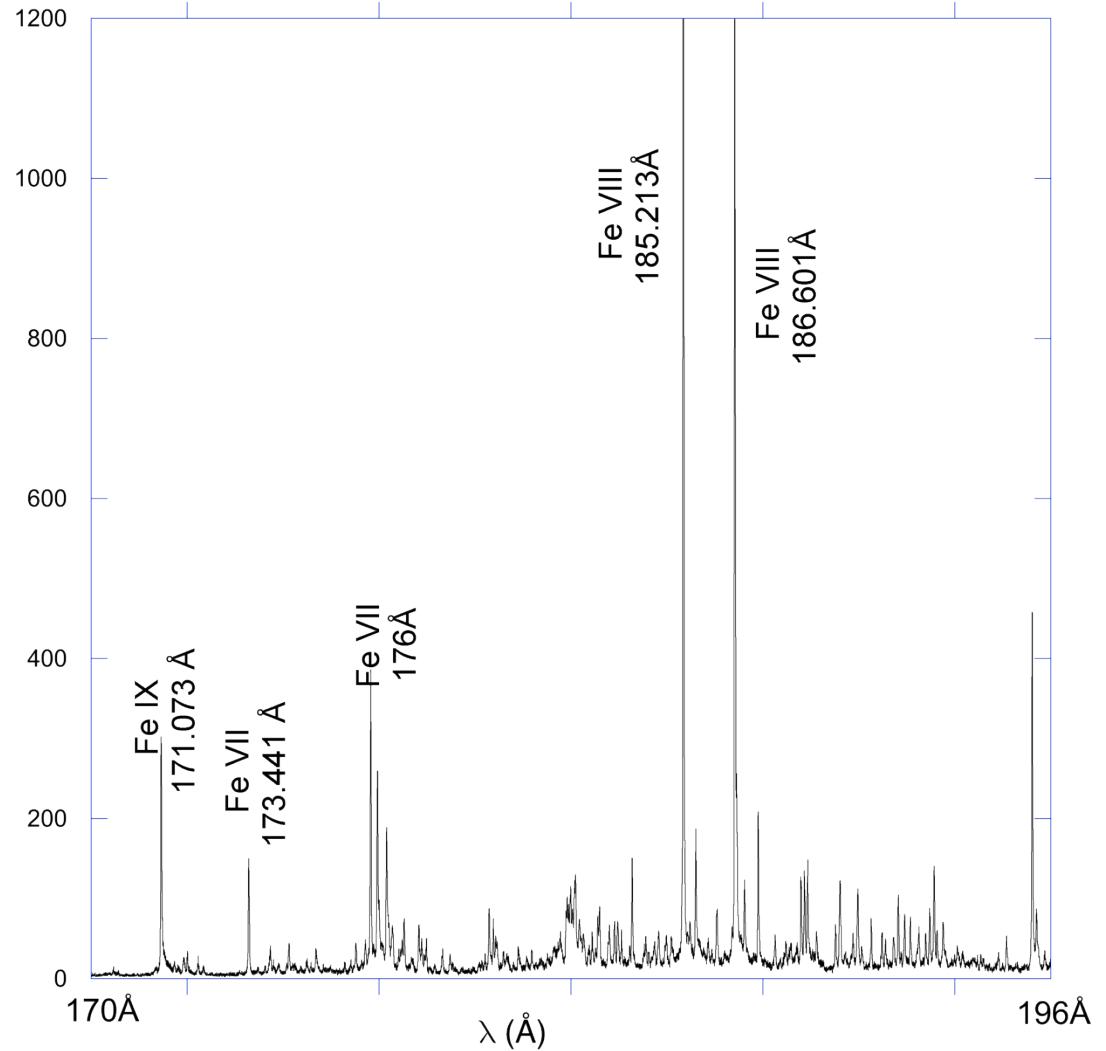
$L=0$

$L=11 \mu\text{H}$

$L=62 \mu\text{H}$

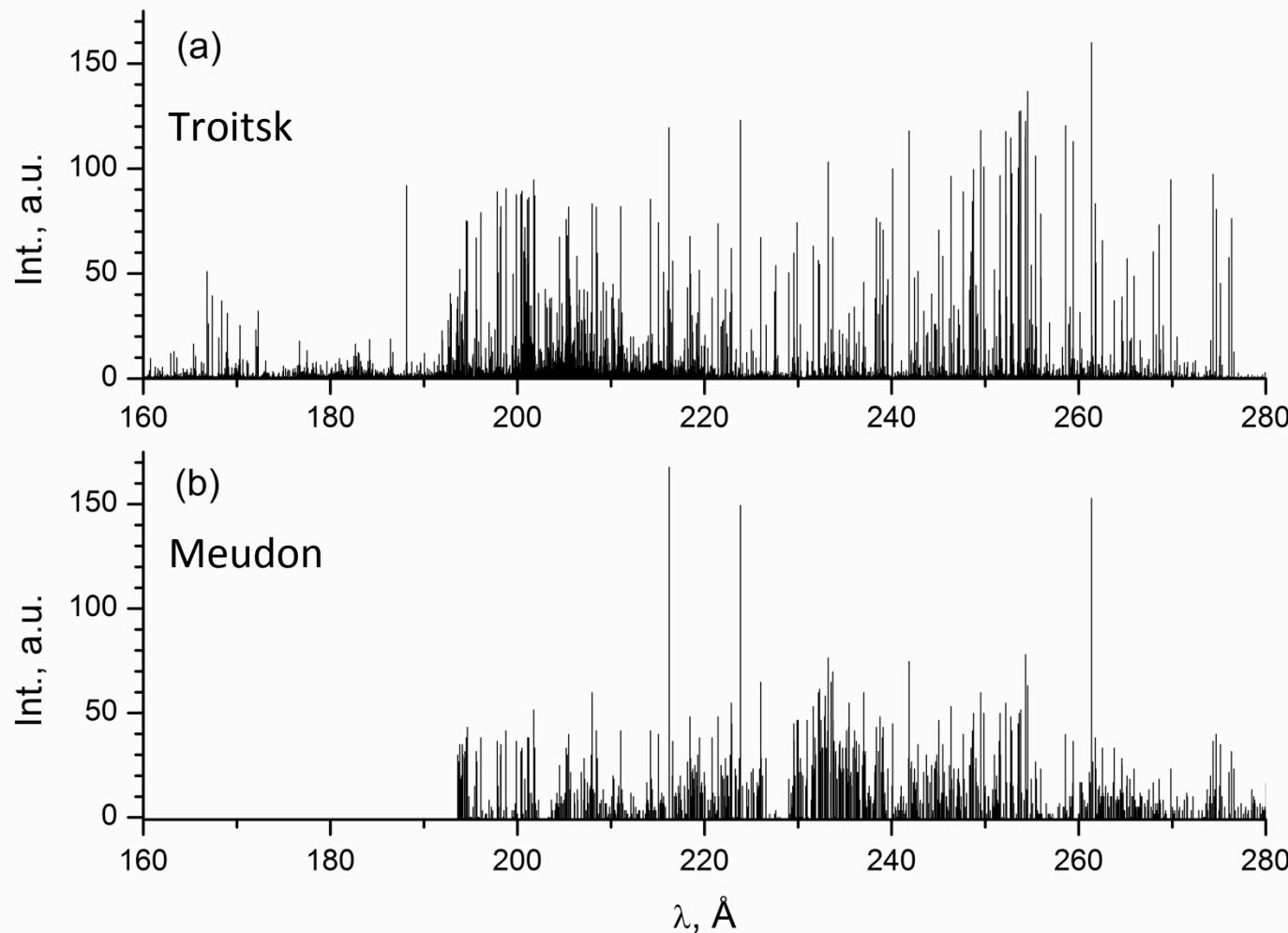
Extension vers les courtes λ ($\sim 165\text{\AA}$)
Recouvrement avec incidence rasante

Fe spark spectrum



Short λ overlap

(a) Troitsk **grazing incidence** spectrograph ; (b) Meudon **normal incidence** spectrograph



Ionized W spectra : Vacuum spark source

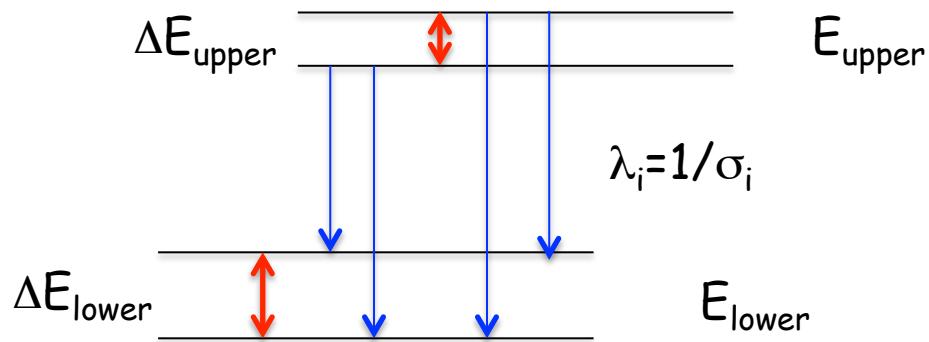
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Analysis: to build the energy level scheme from lines

Ritz combination principle :
 $\sigma = (\lambda)^{-1} = E_{\text{upper}} - E_{\text{lower}} \text{ (cm}^{-1}\text{)}$

+
Selection rules



!! Line intensities \leftrightarrow calculated transition probabilities gA

A long trial and error procedure sped up by the IDEN code
(Azarov 1991 & 1993)

$\Rightarrow E_{\text{exp}}$, identification of $\lambda_{\text{measured}}$

Optimization of all E_{exp} values from all $\lambda_{\text{measured}}$ of identified transitions
(LOPT code, Kramida 2011)

\Rightarrow Precise Ritz λ for allowed and forbidden lines $\lambda_{\text{Ritz}} = (E_u^{\text{opt}} - E_l^{\text{opt}})^{-1}$

Theoretical Method (Racah-Slater) RCN/RCG/**RCE** codes by R.D. Cowan

HFR

$$H = H_0 + H_1$$

H_0 : central field hamiltonian \Rightarrow
Hartree-Fock solution for orbitals and E_{average} for configurations

$$H_1 = Q + \Lambda = \text{electrostatic interactions} + \text{relativistic corrections (spin-orbit)}$$

- Diagonalization : basis of one or several configurations (CI)
- \Rightarrow Predicted energies and wavefunctions
- \Rightarrow Calculation of transition integrals : $gA \leftrightarrow$ predicted intensities

Semi-empirical approach (RCE)

matrix element : $H_{1ij} = \sum_{\alpha} c_{ij}^{\alpha} P_{\alpha}$

c_{ij}^{α} : angular part \rightarrow Racah algebra

P_{α} : radial integral \rightarrow adjustable energy parameters

- iterative least squares fits of P_{α} to minimize $\Delta E = \sqrt{\sum_i (E_i^{\text{exp}} - E_i^{\text{cal.}})^2 / (N_i - N_p)}$

Initial values of P_{α} : HFR values or multiplied by a scaling factor

Atomic Number	Ground-state Level												
Symbol	58	Ce	1G_4										
Name	Cerium												
Standard Atomic Weight [†]	140.116		$[Xe]4f5d6s^2$										
Ground-state Configuration			5.5386										
Ionization Energy (eV)													

Lanthanides

57	$^2D_{3/2}$	58	1G_4	59	$^{4f}_{9/2}$	60	5I_4	61	$^6H_{5/2}$	62	7F_0	63	$^8S_{1/2}$	64	9D_2	65	$^6H_{15/2}$	66	5I_8	67	$^{4f}_{15/2}$	68	5H_6	69	$^2F_{7/2}$	70	1S_0	71	$^{2D}_{3/2}$	
La		Ce		Pr		Nd		Pm		Sm		Eu		Gd		Tb		Dy		Ho		Er		Tm		Yb		Lu		
Lanthanum	138.90547	Cerium	140.116	Praseodymium	140.907	Neodymium	144.242	Promethium	(145)	Samarium	150.36	Europium	151.964	Gadolinium	157.25	Terbium	162.500	Dysprosium	164.93033	Holmium	168.93422	Erbium	173.054	Thulium	174.9668	Ytterbium	174.9668	Lutetium	174.9668	
	[Xe]5d6s ²			[Xe]4f ¹ 6s ²		[Xe]5d250		[Xe]4f ¹ 6s ²		[Xe]4f ¹ 6s ²		[Xe]4f ¹ 6s ²		[Xe]4f ¹ 6s ²		[Xe]4f ¹ 5d6s ²		[Xe]4f ¹ 6s ²		[Xe]4f ¹ 6s ²		[Xe]4f ¹ 6s ²		[Xe]4f ¹ 6s ²		[Xe]4f ¹ 6s ²		[Xe]4f ¹ 6s ²		
	5.5769		5.5386	5.473		5.5250				5.6437		5.6704		5.6838		6.1498		6.1498		6.0215		6.1077		6.1843		6.2542		5.4259		

Actinides

89	$^2D_{3/2}$	90	3F_2	91	$^{4K}_{11/2}$	92	5L_6	93	$^6L_{11/2}$	94	7F_0	95	$^8S_{7/2}$	96	9D_2	97	$^6H_{15/2}$	98	5I_8	99	$^{4I}_{15/2}$	100	3H_6	101	$^2F_{7/2}$	102	1S_0	103	$^{2P}_{1/2}$		
Ac		Th		Pa		U		Np		Pu		Am		Cm		Bk		Cf		Es		Fm		Md		No		Lr		Lu	
Actinium	(227)	Thorium	232.0377	Protactinium	231.03588	Uranium	238.02891	Neptunium	(237)	Plutonium	(244)	Americium	(243)	Curium	(247)	Berkelium	(247)	Californium	(251)	Einsteinium	(252)	Fermium	(258)	Mendelevium	(259)	Nobelium	(262)	Lawrencium	(262)	Lutetium	(262)
	[Rn]6d7s ²		6.3067	[Rn]6d ² 7s ²		5.89		[Rn]5f ³ 6d7s ²		[Rn]5f ⁴ 6d7s ²		[Rn]5f ⁴ 7s ²		[Rn]5f ⁵ 6d7s ²		[Rn]5f ⁵ 6d7s ²		[Rn]5f ⁶ 7s ²		[Rn]5f ⁷ 7s ²		[Rn]5f ¹² 7s ²		6.58		[Rn]5f ¹⁴ 7s ²		6.65			

*Based upon ^{12}C . () indicates the mass number of the longest-lived isotope.

*IUPAC conventional atomic weights; standard atomic weights for these elements are expressed in intervals; see iupac.org for an explanation and values.

For a description of the data, visit physics.nist.gov/data
NIST SP 966 (September 2014)

Er IV

ground configuration $5p^64f^{11}$

isoionic

excited
core excited

$5p^64f^{10} 5d, 6s, 6p\dots$
 $5p^54f^{11} 5d, 6s, 6p\dots$

Previous analysis by Carter (thesis 1966) needs complete revision
MCDHF calculations by Radžiutė et al (2015)

Tm IV

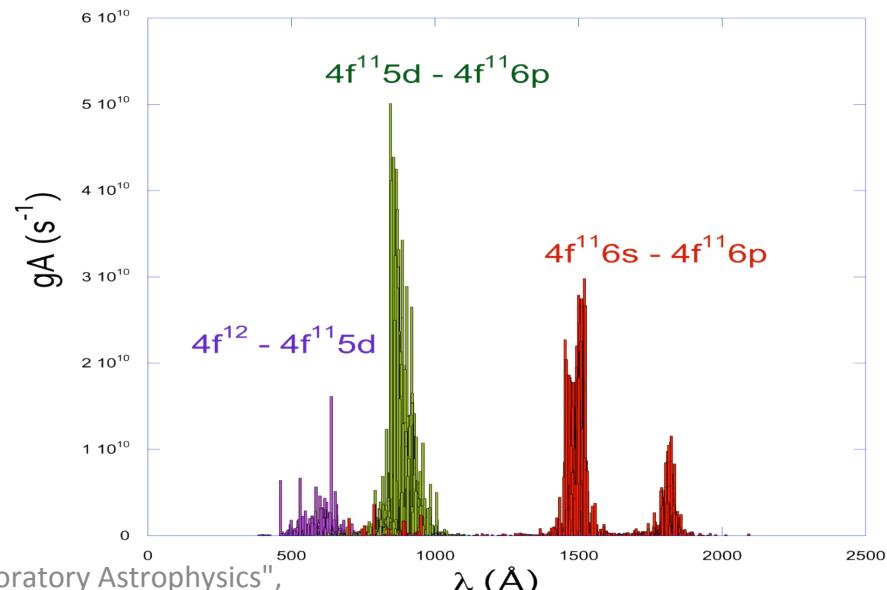
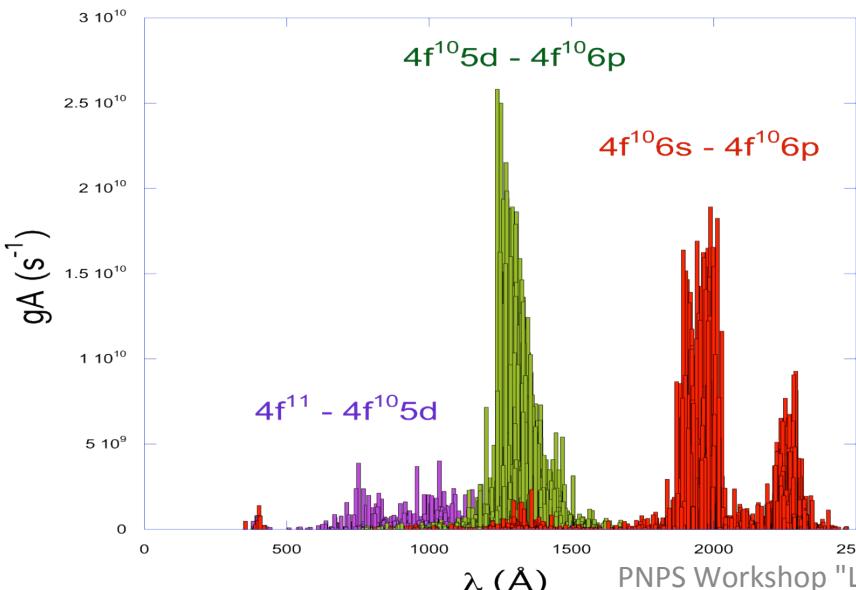
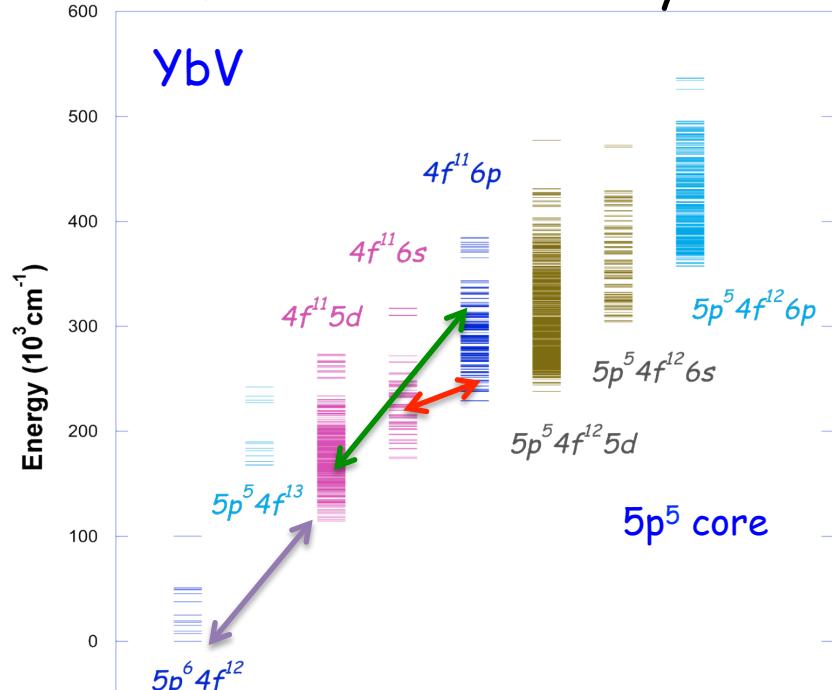
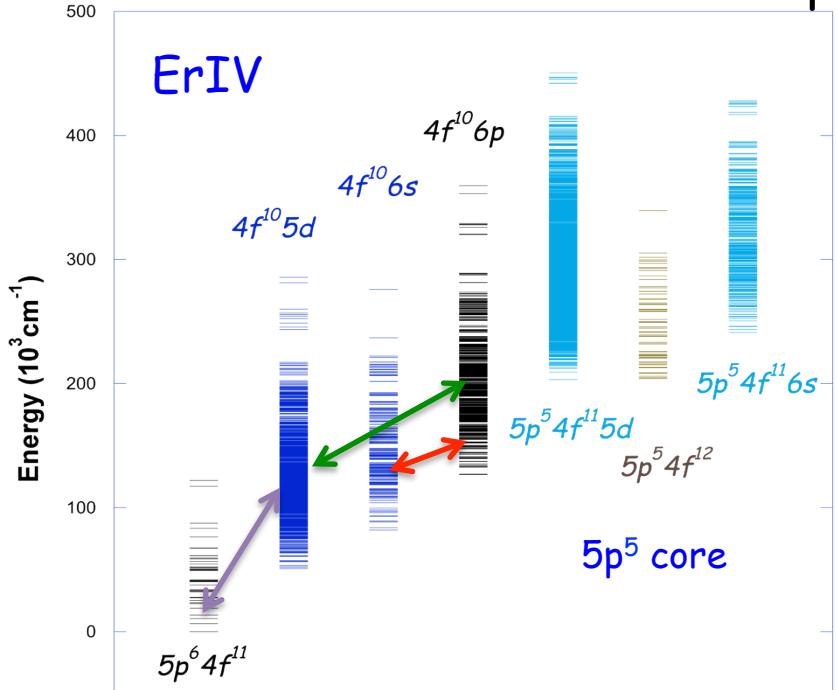
Meftah et al.
Phys. Scr. 2008

isoelectronic

Yb V previously unknown

ground configuration $5p^64f^{12}$,
excited $5p^64f^{11} 5d, 6s, 6p\dots$
core excited $5p^54f^{12} 5d, 6s, 6p\dots$

Relativistic Hartree-Fock predictions for transition arrays



Consistency of scaling factor (SF) values $SF = P_{\text{fit}} / P_{\text{HFR}}$ and effective CI parameters

Parameters	Nd IV	Nd V	Tm IV	Er II	Yb V	Er IV
	$4f^3 + \dots$	$4f^2 + 4f6p$	$4f^{12} + 4f^{11}6p$	$4f^{12}6p$	$4f^{12} + 4f^{11}6p$	$4f^{11} + 4f^{10}6p$
	$4f^25d + \dots$	$4f5d + \dots$	$4f^{11}5d + \dots$	$4f^{12}5d + \dots$	$4f^{11}5d + \dots$	$4f^{10}5d + \dots$
$F^2(4f,4f)$	0.768	0.761	0.785	0.763	0.800	0.779
$F^4(4f,4f)$	0.839	0.852	0.868	0.844	0.898	0.880
$F^6(4f,4f)$	0.797	0.766	0.855	0.930	0.864	0.877
ζ_{4f}	0.932	0.927	0.982	0.981	0.982	0.991
$F^2(4f,5d)$	0.758	0.763	0.806	0.816	0.807	0.804
$F^4(4f,5d)$	1.082	1.100	1.132	1.174	1.129	1.152
$G^1(4f,5d)$	0.846	0.860	0.751	0.683	0.774	0.693
$G^3(4f,5d)$	0.954	0.983	0.974	1.013	0.960	0.966
$G^5(4f,5d)$	0.839	0.868	0.830	0.753	0.843	0.822
$F^2(4f,6p)$	0.797	0.815	0.867	0.820	0.844	0.803
ζ_{6p}	1.207	1.168	1.17	1.320	1.143	1.173
Effective CI parameter						
$F^1(4f,5d)$	758±57	839±147	866±106	902±62	819±81	1066±109

Fitted Energy Parameters Yb V Even parity

$4f^{12}, 4f^{11}6p$
 $5p^54f^{13}, 5p^54f^{12}6p$

56 Eexp
 $N_p=21$
 $RMS=55 \text{ cm}^{-1}$

$$SF = P_{\text{fit}} / P_{\text{HFR}}$$

CI parameters



Param.	$4f^{12}$				$4f^{11}6p$			
	Fitted	St.dev.	HFR	SF	Fitted	St.dev.	HFR	SF
E_{av}	20531	17			300546	35	264316	
$F^2(4f4f)$ r	114180	175	142711	0.800	119139	183	148907	0.800
$F^4(4f4f)$ r	80688	377	89854	0.898	84488	395	94085	0.898
$F^6(4f4f)$ r	55929	267	64733	0.864	58646	280	67877	0.864
α	17.9	2			21.7	3		
β r	-738	86			-738	86		
γ r	1757	104			1757	104		
ζ_{4f} r	3066	6	3121	0.982	3228	6	3287	0.982
ζ_{6p}					7739	16	6777	1.143
$F^1(4f6p)$					270	85		
$F^2(4f6p)$					9625	283	11403	0.844
$G^2(4f6p)$					2939	88	2919	1.007
$G^4(4f6p)$					2560	233	2677	0.956

Param.	$5p^54f^{13}$				$5p^54f^{12}6p$			
	Fitted	St.dev.	HFR	SF	Fitted	St.dev.	HFR	SF
E_{av}	192408	f	172089		412123	f	391804	
$F^2(4f4f)$					113153	f	144145	
$F^4(4f4f)$					79482	f	90836	
$F^6(4f4f)$					56625	f	65463	
α					17	f		
β					-653	f		
γ					1712	f		
ζ_{4f}	2932	f	2986	0.982	3090	f	3147	0.982
ζ_{5p}	35833	f	35833	1.000	39067	f	39067	1.000
ζ_{6p}					7881	f	6736	1.169
$F^1(5p4f)$	1000	f				f		
$F^2(5p4f)$	46397	f	57796	0.800	47896	f	59871	0.800
$F^1(4f6p)$		f			100	f		
$F^2(4f6p)$		f			10120	f	11627	0.870
$F^1(5p6p)$		f				f		
$F^2(5p6p)$		f			17729	f	22162	0.800
$G^2(5p4f)$	22571	f	28213	0.800	22176	f	27721	0.960
$G^4(5p4f)$	17677		22096	0.800	17688	f	22110	0.800
$G^2(4f6p)$					3054	f	3054	1.000
$G^4(4f6p)$					2509	f	2788	0.900
$G^0(5p6p)$					3332	f	4165	0.800
$G^2(5p6p)$					4689	f	5862	0.800
C.I. Parameter	Fitted	St.dev.	HFR	SF				
$5p^64f^{12} - 5p^54f^{13}$								
$R^2(4f5p, 4f4f)$	-10022	f	-15745	(0.700)				
$R^4(4f4f, 4f5p)$	-4279	f	-6113	(0.700)				
$R^2(5p5p, 4f5p)$	-28260	f	-40371	(0.700)				
$5p^64f^{12} - 5p^64f^{11}6p$								
$R^2(4f4f, 4f6p)$	-2278	f	-3254	(0.700)				
$R^4(4f4f, 4f6p)$	-1092	f	-1560	(0.700)				
$5p^64f^{12} - 5p^54f^{12}6p$								
$R^2(4f5p, 4f6p)$	11025	f	15750	(0.700)				
$R^2(4f5p, 6p4f)$	5692	f	8132	(0.700)				
$R^4(4f5p, 6p4f)$	4903	f	7004	(0.700)				
$R^2(5p5p, 5p6p)$	7380	f	10543	(0.700)				

r : all the parameters of the same group are linked by a constant ratio
f : fixed parameter

Nov. 15-16, 2016, Lyon

Mean error of the fit = 55 cm^{-1}

Nd V core-excited configuration

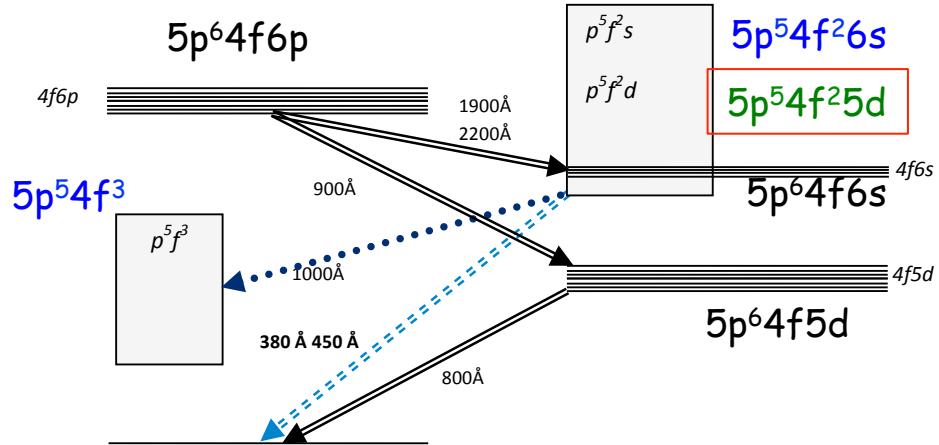
$5p^54f^25d$

(Deghiche et al 2015)

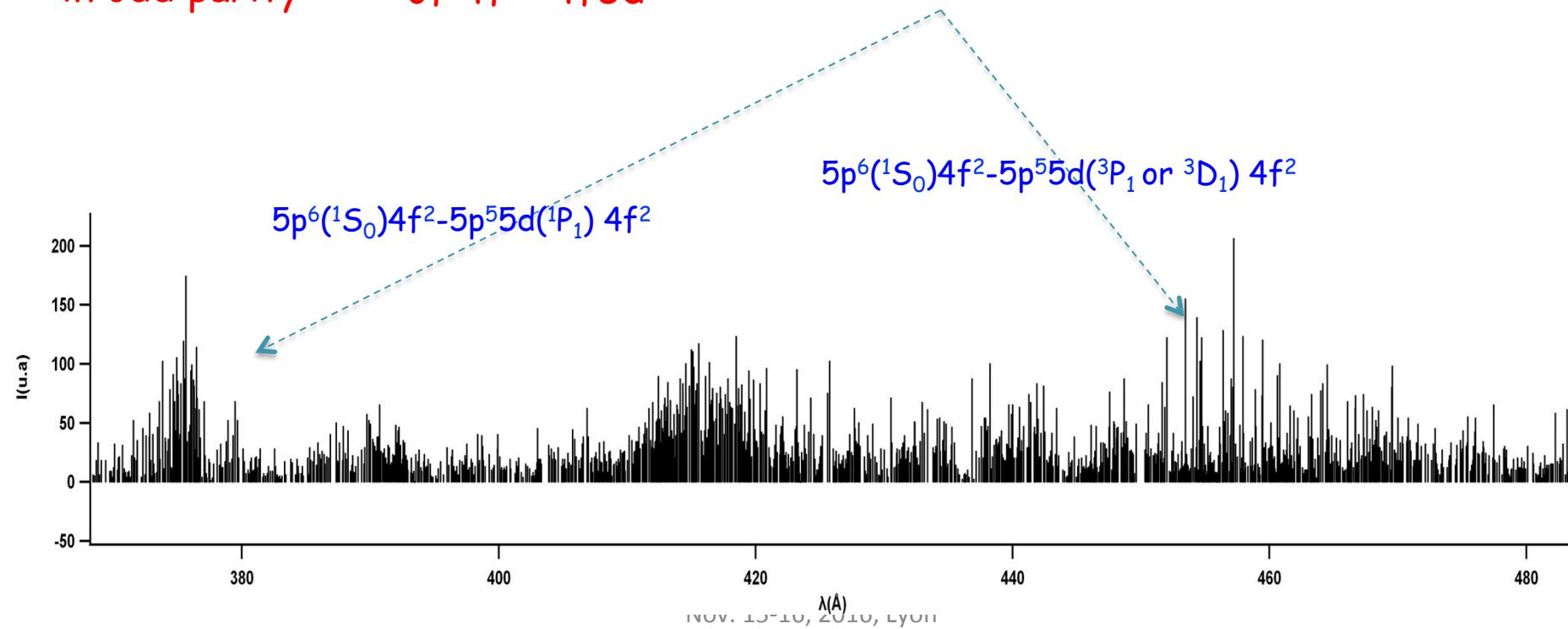
305 lines

λ (350 - 550 Å)

104 energy levels



Strong CI
in odd parity → Intensity reduction
of 4f²- 4f5d



Comparison : experimental and calculated wavelengths and intensities

Cal. HFR

Nd⁴⁺

Nd V, 12 configurations basis, transitions 4f²-4f5d and 4f5d-4f6p assumed T= 3.5 eV

Exp.

phosphor image plate Nd sliding spark spectrum

Cal. final param.

4f5d-4f6p

4f² -4f5d

Intensity (arb. units)

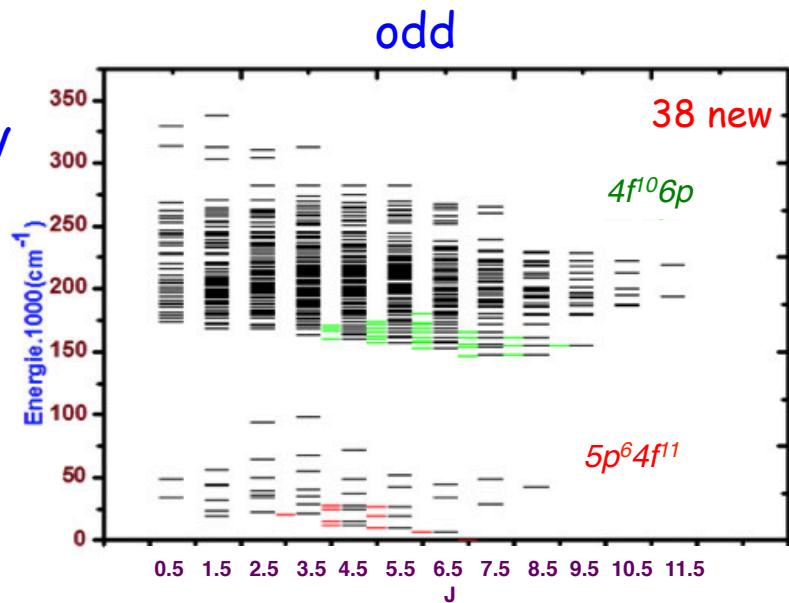
870 880 890 900 910 920 930

wavelength (Å)

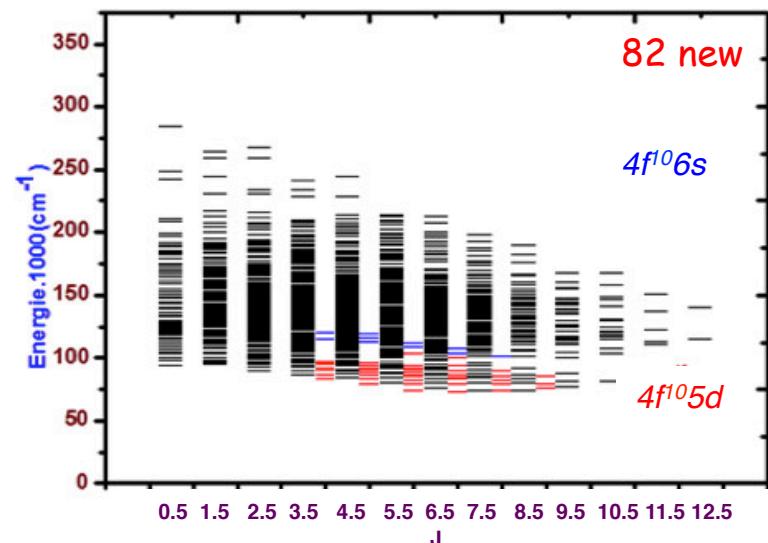
Results on energy levels

calc. (black) and exp. (color)

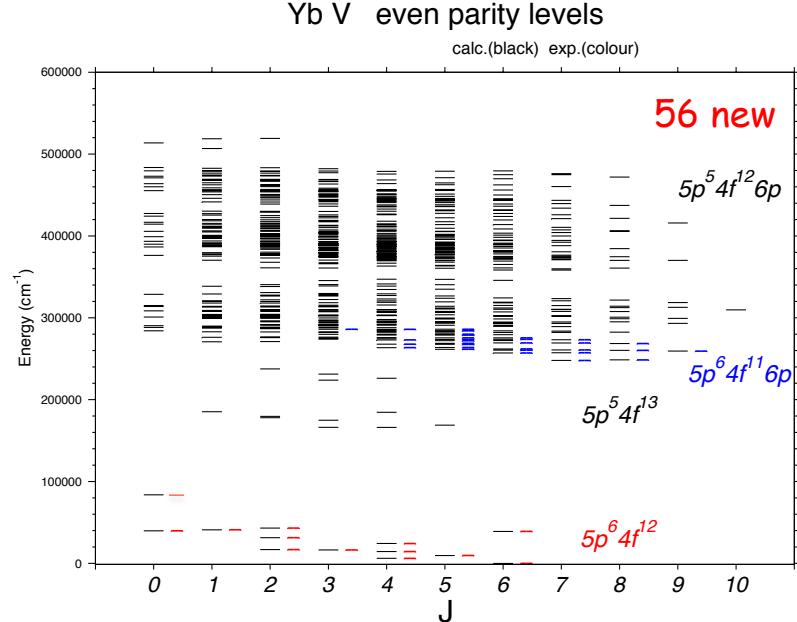
ErIV



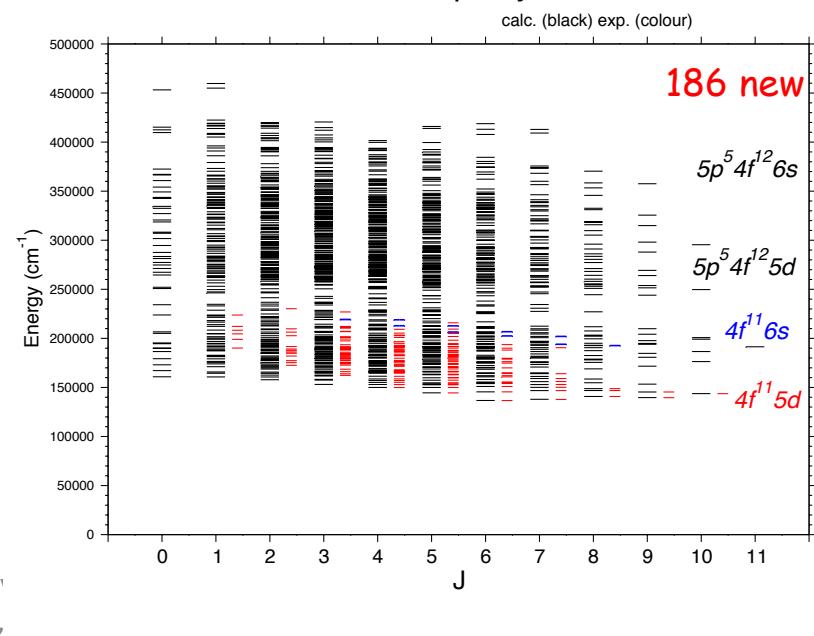
even



YbV

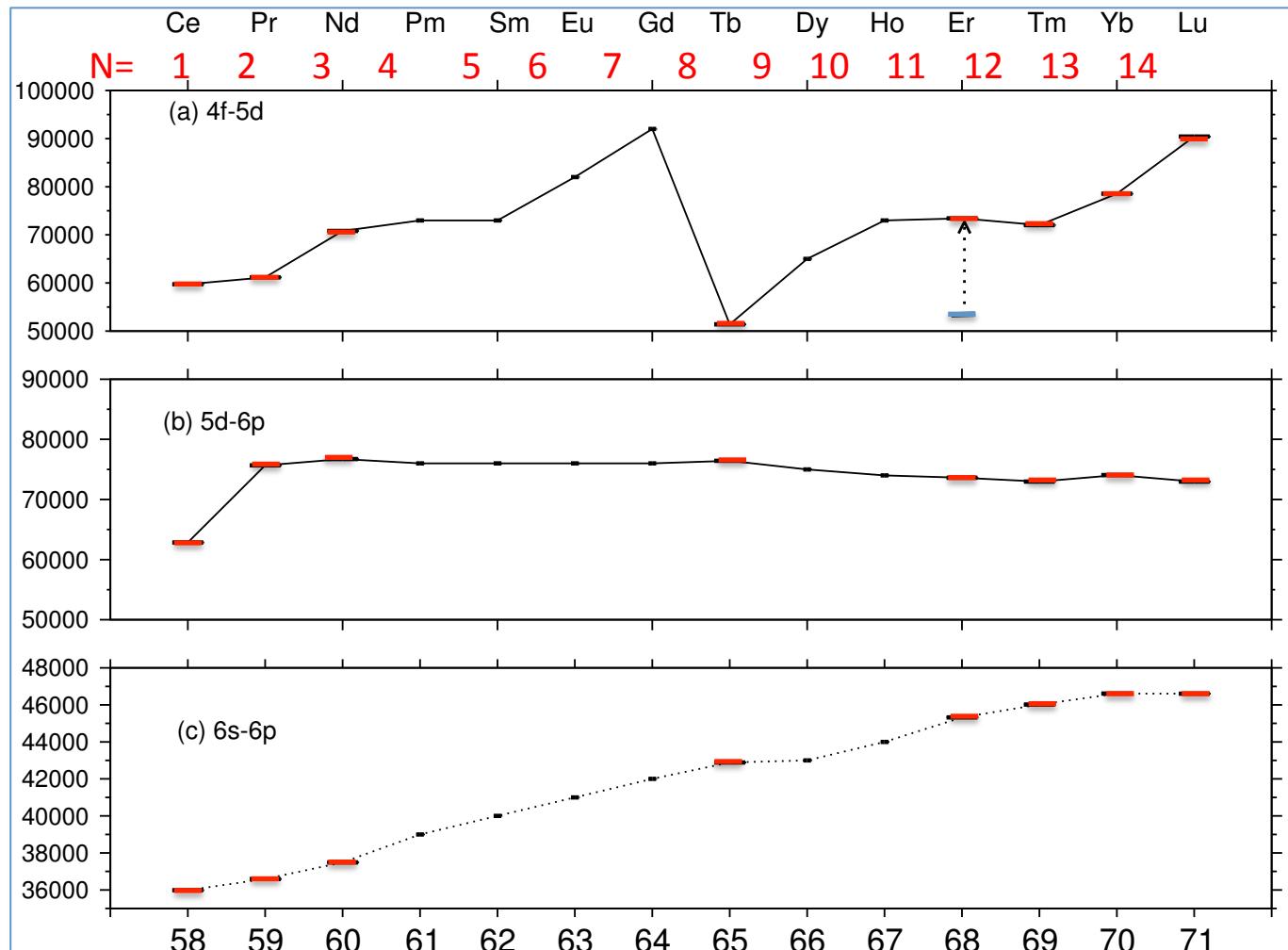


Yb V odd parity levels



Energy interval between the lowest levels of the main configurations in all triply ionized lanthanides Ln^{3+}

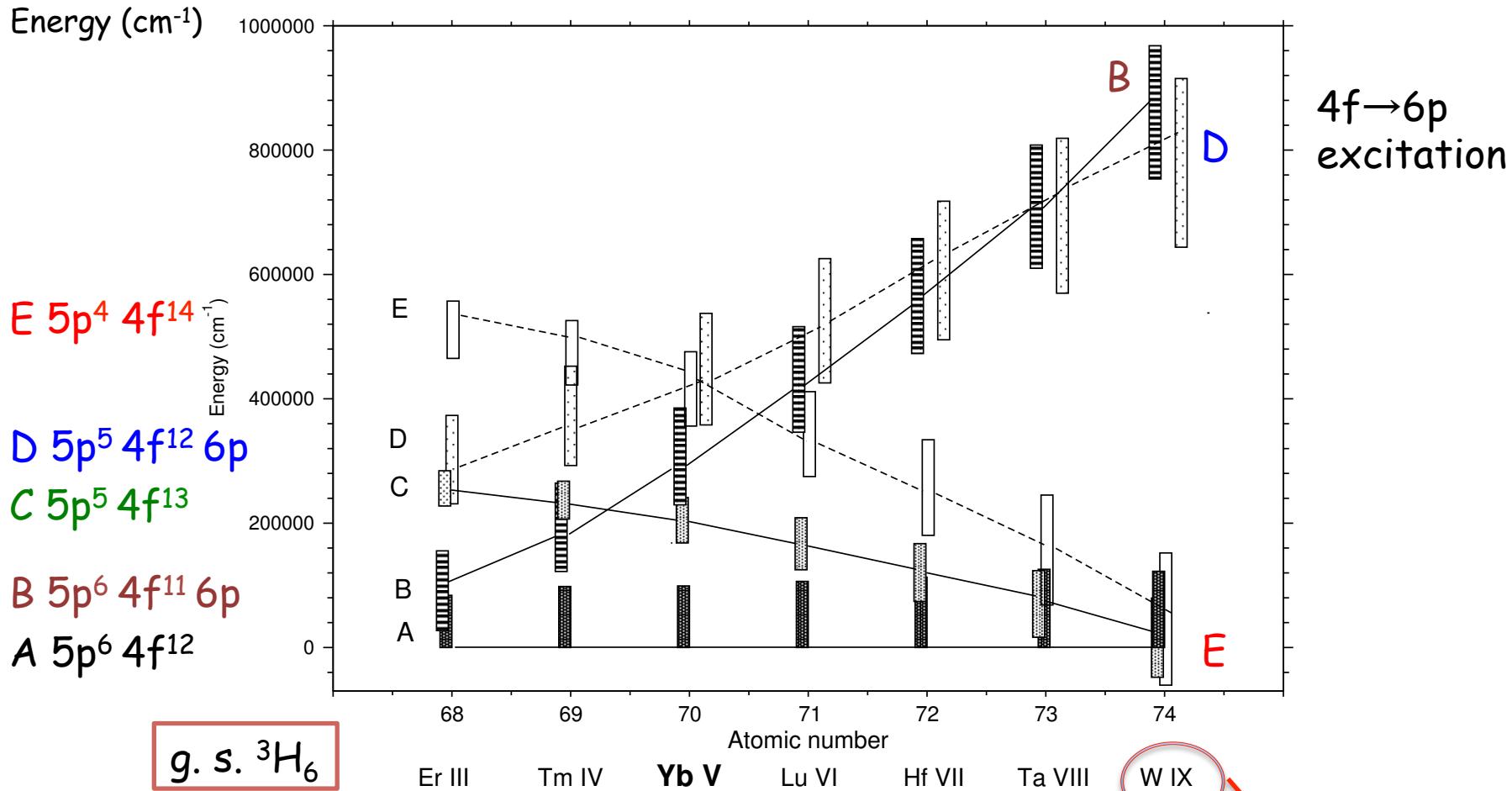
$4f^N - 4f^{N-1} 5d$



— Experimentally known

Energy ranges of even configurations
in the Dy I isoelectronic sequence → W IX

$5p \rightarrow 4f$ excitation $\varepsilon \searrow \Rightarrow 5p^6 4f^N - 5p^5 4f^{N+1}$ cores overlap



U II : Results of the Least Squares Fits (RCE)

Odd parity 253 experimental E, 24 free parameters, 62 constrained ones
Root Mean Square 60 cm⁻¹

Even parity 125 experimental E, 22 free parameters 39 constrained ones
Root Mean Square 84 cm⁻¹

Partition function for a typical stellar temperature

$$T = 4825 \text{ K} \Leftrightarrow k_B T = 3353.541 \text{ cm}^{-1}$$

$$Q(T) = \sum_i (2J+1) \exp\left(-\frac{E_i}{k_B T}\right)$$

k_B : Boltzmann Constant

Taking into account all $E_i < 50\,000 \text{ cm}^{-1}$

Odd + even levels

Experimental energies : $Q = 109.67 + 13.32 = 122.99$

Calculated energies after LSF :

$$Q = 107.84 + 13.15 = 120.99 \quad \Delta \sim 2\%$$

Ab initio HFR calculations :

$$Q = 87.13 + 2.06 = 89.19 \quad \Delta \sim 28\%$$

Table 3: Energy levels of U II, odd parity. Comparison of experimental energies and Landé factors with values calculated from the parameter set of Table 1. The configuration percentage is reported in the last five columns.

J	E^{exp}	E^{th}	ΔE	g_L^{th}	g_L^{exp}	%	1 st conf.	Comp.	f^3ds	f^3d^2	f^3s^2	f^4p	f^5	Note
4.5	0.000	-66.3	66	0.757	0.765	76	f3.s2	(4I)4I	3.39	4.88	91.71	0.01	0.01	
5.5	289.041	218.3	70	0.656	0.655	77	f3.ds	(4I)6L	99.85	0.14	0	0	0	
4.5	914.765	923.6	-8	0.604	0.605	71	f3.ds	(4I)6K	96.26	0.85	2.58	0.31	0	
6.5	1749.123	1717.8	31	0.864	0.865	45	f3.ds	(4I)6L	93.82	6.15	0.03	0	0	
5.5	2294.696	2317.5	-22	0.868	0.865	47	f3.ds	(4I)6K	97.49	1.82	0.40	0.20	0	
5.5	4420.871	4410.9	9	0.971	0.97	89	f3.s2	(4I)4I	1.43	4.99	93.56	0	0.01	
6.5	4585.434	4585.0	0	0.793	0.785	28	f3.d2	(4I)6M	48.11	51.84	0.05	0	0	
2.5	4706.273	4649.5	56	0.478	0.480	32	f3.ds	(4I)6H	96.78	1.69	1.16	0.37	0.01	
7.5	5259.653	5247.5	12	1.007	1.015	68	f3.ds	(4I)6L	97.57	2.42	0.01	0	0	
3.5	5401.503	5344.6	56	0.801	0.690	20	f3.ds	(4I)6I	98.10	1.07	0.06	0.77	0	
6.5	5526.750	5552.3	-25	1.019	1.020	70	f3.ds	(4I)6K	98.28	1.32	0.12	0.28	0	
3.5	5667.331	5700.7	-33	0.623	0.735	57	f3.ds	(4I)6I	96.89	1.41	0.12	1.58	0	
5.5	5790.641	5832.7	-42	0.852	0.860	39	f3.ds	(4I)6K	95.52	4.06	0.06	0.36	0	
6.5	6283.431	6395.7	-112	0.786	0.790	38	f3.d2	(4I)6M	54.49	45.37	0.13	0.01	0	
4.5	6445.035	6487.7	-42	0.832	0.840	43	f3.ds	(4I)6I	97.65	0.63	0.15	1.58	0	
0.5		6933.0		2.394		20	f3.ds	(4F)4Pa	97.75	2.19	0.02	0.04	0	
1.5	7017.172	7087.3	-70	0.611	0.620	59	f3.s2	(4F)4F	3.88	5.27	90.81	0.03	0.02	
4.5	7166.632	7255.5	-88	0.951	0.940	20	f3.ds	(4I)6H	95.20	4.14	0.10	0.56	0	
3.5	7547.374	7614.9	-67	0.802	0.790	21	f3.ds	(4I)4Ha	84.63	14.61	0.15	0.61	0	
5.5	7598.353	7615.6	-17	0.971	0.980	18	f3.ds	(4I)4Ia	98.01	1.48	0.02	0.49	0	
6.5	8276.733	8259.7	17	1.093	1.090	84	f3.s2	(4I)4I	4.92	5.13	89.93	0.01	0.01	
4.5	8379.697	8357.6	22	0.838	0.840	14	f3.ds	(4I)6I	75.96	21.67	1.74	0.62	0.01	
1.5	8400.125	8432.2	-32	0.086	0.150	68	f3.ds	(4I)6G	97.66	0.96	0.51	0.87	0	
2.5	8430.185	8438.3	-8	0.719	0.720	38	f3.ds	(4I)6G	94.18	1.86	3.22	0.72	0.02	
7.5	8394.362	8444.8	-50	1.057	0.960	56	f3.ds	(4I)6K	74.24	25.52	0.04	0.21	0	
5.5	8510.866	8467.4	43	0.855	0.860	11	f3.ds	(4I)4Kb	78.67	21.18	0.02	0.13	0	
7.5	8521.922	8542.0	-20	0.963	1.060	42	f3.d2	(4I)6M	42.79	57.13	0.01	0	0	
6.5	8755.640	8764.1	-8	1.043	1.040	14	f3.ds	(4I)4Lb	92.23	4.90	2.66	0.21	0	
8.5	8853.748	8820.3	33	1.105	1.105	83	f3.ds	(4I)6L	98.62	1.38	0	0	0	
3.5	9075.732	9010.2	66	0.873	0.870	15	f3.ds	(4I)6H	68.32	30.46	0.83	0.39	0.01	
2.5	9344.625	9245.1	99	0.754	0.79	25	f3.s2	(4G)4G	42.57	8.68	48.15	0.35	0.26	
4.5	9241.971	9249.9	-7	1.028	1.015	12	f3.ds	(4I)6H	76.03	5.71	17.65	0.60	0.01	
5.5	9553.187	9609.9	-56	1.052	1.060	56	f3.ds	(4I)6I	96.38	1.95	0.02	1.65	0	

"Complete" linelist of Eu III

<http://molat.observatoire.psu.fr/~wyart/eu3linelist.html>

Description:

This table contains 23827 transitions of the Eu III spectrum, involving experimentally determined or calculated energy levels. The calculations were carried out by using Cowan's codes, as explained in the paper : "Extended analysis of the Eu III spectrum", by J.-F. Wyart, W.-L. Tchang-Brillet, S. S. Churilov and A.N. Ryabtsev, Astron. & Astrophys. 483, 339-359 (2008).

Range 1: 2000.000- 3360.000: Max. gA = 5.1E+09 sec-1, Min gA = 1.0E+05 sec-1

Range 2: 3360.000- 6010.000: Max. gA = 2.5E+07 sec-1, Min gA = 1.0E+04 sec-1

Range 3: 6010.000- 9999.000: Max. gA = 5.1E+06 sec-1, Min gA = 1.0E+04 sec-1

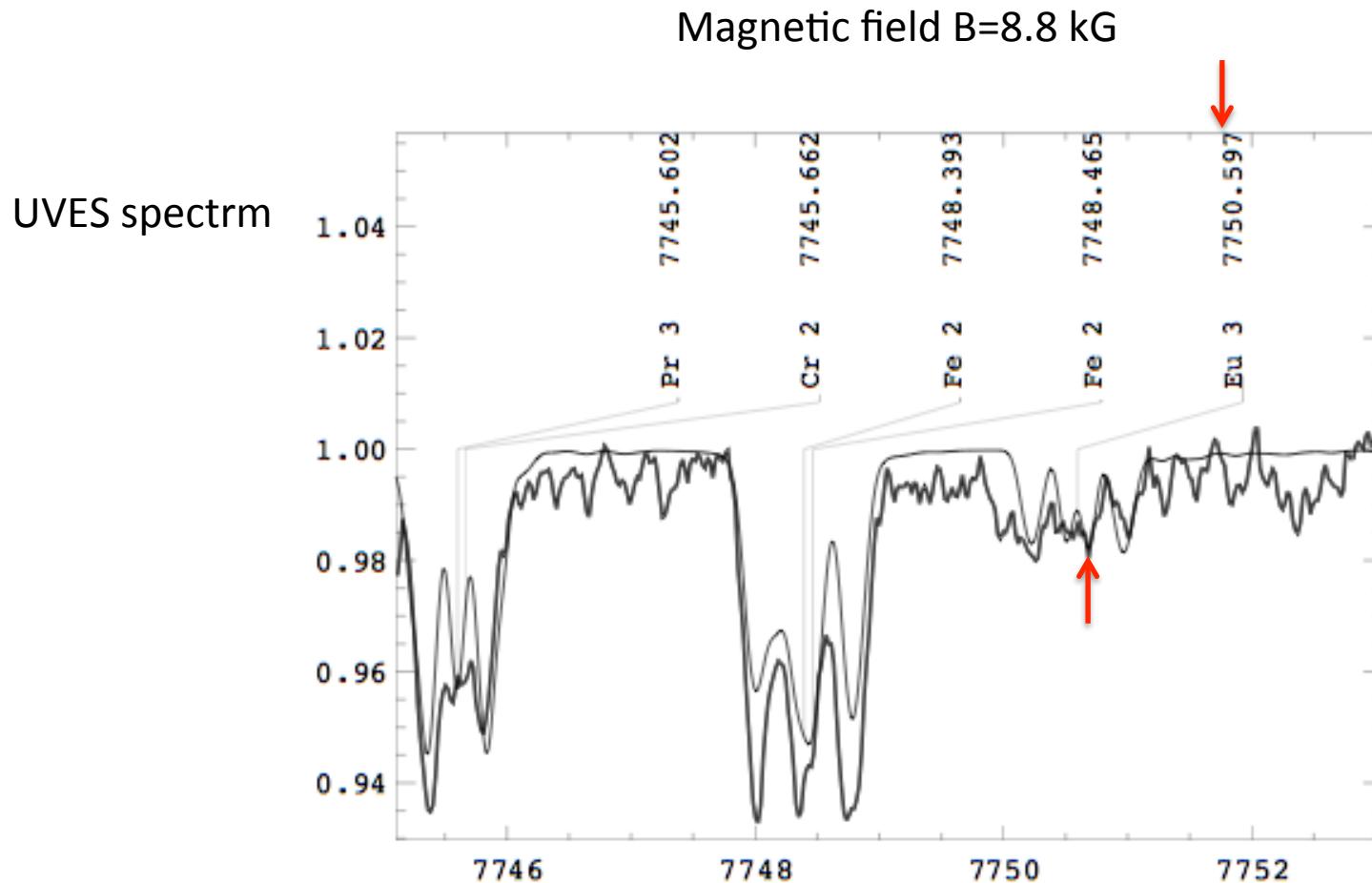
Column

- 1 - 8 Wavelength calculated from level energies (Ritz values)
- 10 - 18 Weighted transition probability (s-1), gu - statistic weight of the upper level
- 20 - 25 Logarithm of weighted oscillator strengths, gl - statistic weight of the lower level
- 28 - 33 Cancellation factor (see R.D.Cowan. Theory of atomic structure and spectra, p.432)
- 35 - 42 Energy of the lower level (cm-1)
- 43 Status of the lower level: * - experimentally measured, otherwise - calculated
- 44 - 46 Parity: e - even, o - odd
- 48 - 53 g - factor Lande
- 55 - 66 Level designation by first component of LS - composition
- 69 - 71 J
- 75 - 82 Energy of the upper level (cm-1)
- 83 Status of the upper level: * - experimentally measured, otherwise - calculated
- 84 - 86 Parity: e - even, o - odd
- 88 - 93 g - factor Lande
- 95 -107 Level designation by first component of LS - composition
- 110 -112 J

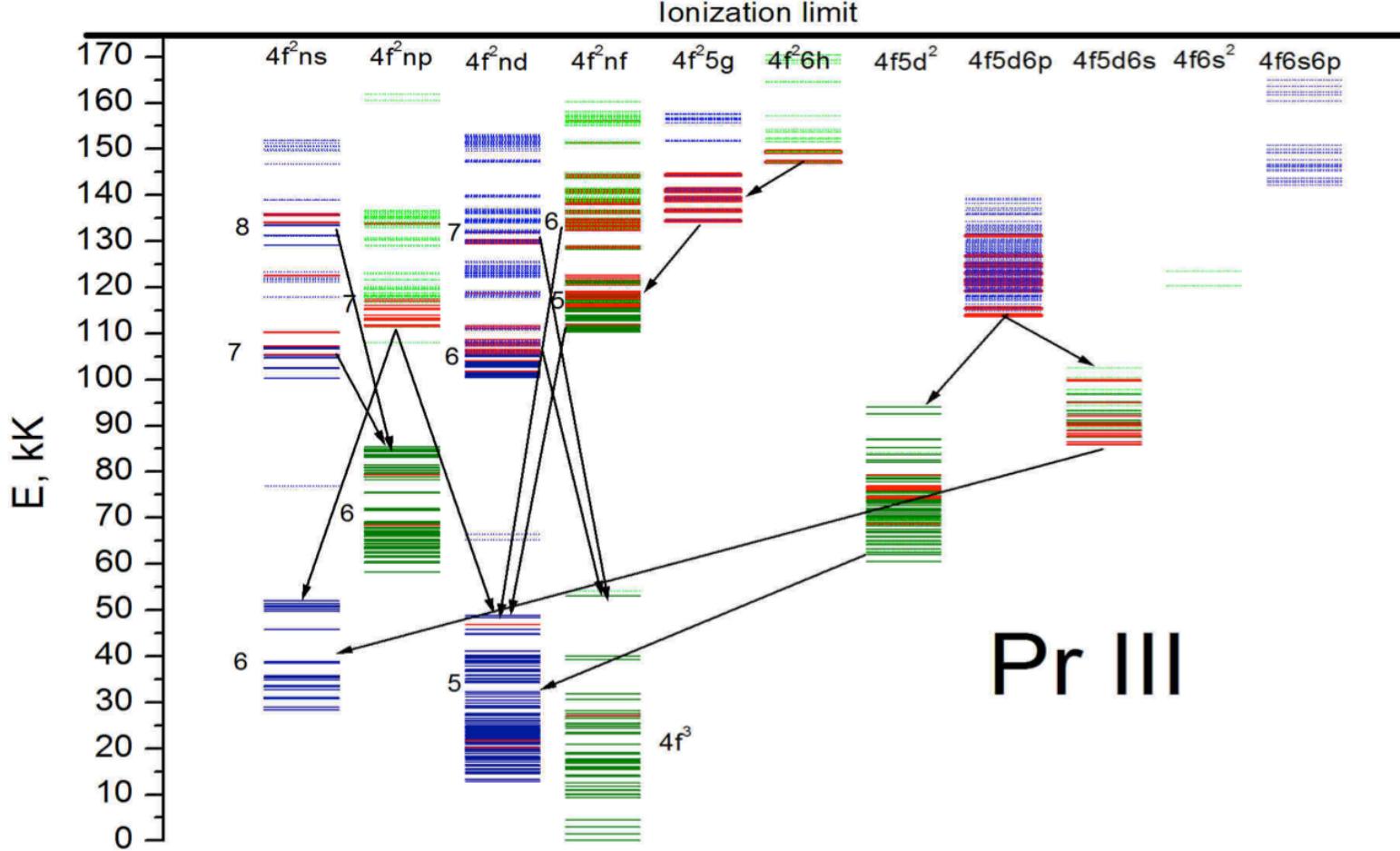
Wyart, Tchang-Brillet, Churilov et al.

Lambda,A	guA	log(glf)	CF	Lower level				Upper level			
				E, cm ⁻¹	g	Name	J	E, cm ⁻¹	g	Name	J
2000.032	2.811E+05	-3.773	-0.020	35262.00	(o)	3.318 4f7	6D	0.5 - 85245.00	(e)	1.182 4f65d	(5D2)4S 1.5
2000.232	2.081E+05	-3.903	0.010	35480.00	(o)	1.667 4f7	6D	2.5 - 85458.00	(e)	1.033 4f65d	(5P)4F 2.5
2000.312	4.092E+05	-3.610	-0.010	35480.00	(o)	1.667 4f7	6D	2.5 - 85456.00	(e)	0.978 4f65d	(3K5)4H 3.5
2000.753	2.045E+05	-3.911	-0.070	28848.00	(o)	2.369 4f7	6P	1.5 - 78813.01	(e)	0.197 4f65d	(5G2)4D 0.5
2000.795	1.928E+06	-2.936	-0.050	28200.06*	(o)	1.691 4f7	6P	3.5 - 78164.00	(e)	1.015 4f65d	(5K)6I 4.5
2000.965	3.308E+05	-3.700	-0.020	32073.30*	(o)	1.292 4f7	6I	8.5 - 82033.00	(e)	1.129 4f65d	(5K)4L 9.5
2000.993	2.295E+07	-1.861	0.290	28848.00	(o)	2.369 4f7	6P	1.5 - 78807.00	(e)	1.375 4f65d	(5D2)6P 2.5
2001.084	2.185E+06	-2.879	-0.220	0.00*	(o)	1.997 4f7	8S	3.5 - 49956.73*	(e)	1.491 4f65d	(7P)6D 4.5
2001.354	1.192E+05	-4.145	-0.010	35338.00	(o)	1.589 4f7	6D	3.5 - 85288.00	(e)	1.057 4f65d	(3P8)2D 2.5
2001.366	4.125E+06	-2.604	0.090	32073.30*	(o)	1.292 4f7	6I	8.5 - 82023.00	(e)	1.185 4f668	(5I2)6I 7.5
2001.526	2.086E+06	-2.902	0.150	36962.29*	(e)	1.298 4f65d(7F)8H	5.5	86908.00	(o)	0.971 4f7	2H9 4.5
2001.859	2.434E+07	-1.834	-0.040	38229.07*	(e)	1.790 4f65d(7F)8D	3.5	88166.46*	(o)	1.524 4f66p	(7P)6D 4.5

Results used for identification of Eu III lines in Ap star
HD 144897 and determination of Eu abundance



Comparison between the observed spectrum of HD 144897 in the region of Eu III $\lambda 7750.59$ Å line (double line) and synthesized spectrum with the atomic parameters derived in the present work (full line).



Experimental data : 7300 lines (821 - 10717 Å)

New analysis : ~ 4900 classified = from high lying levels of $4f^27p$, $4f^27d$, $4f^26f$, $4f^25g$, $4f^26h$ and $4f5d6p$ configurations

Determination of 403 odd levels (prev. 234) and 235 even levels (167).

Parametric studies : odd $4f^3$ + $4f^26p$ + $4f^27p$ + $4f^55d^2$ + $4f5d6s$ + $4f6s^2$ +
 $4f^25f$ + f^26f + $5p^57f$ + $5p^54f^36p$

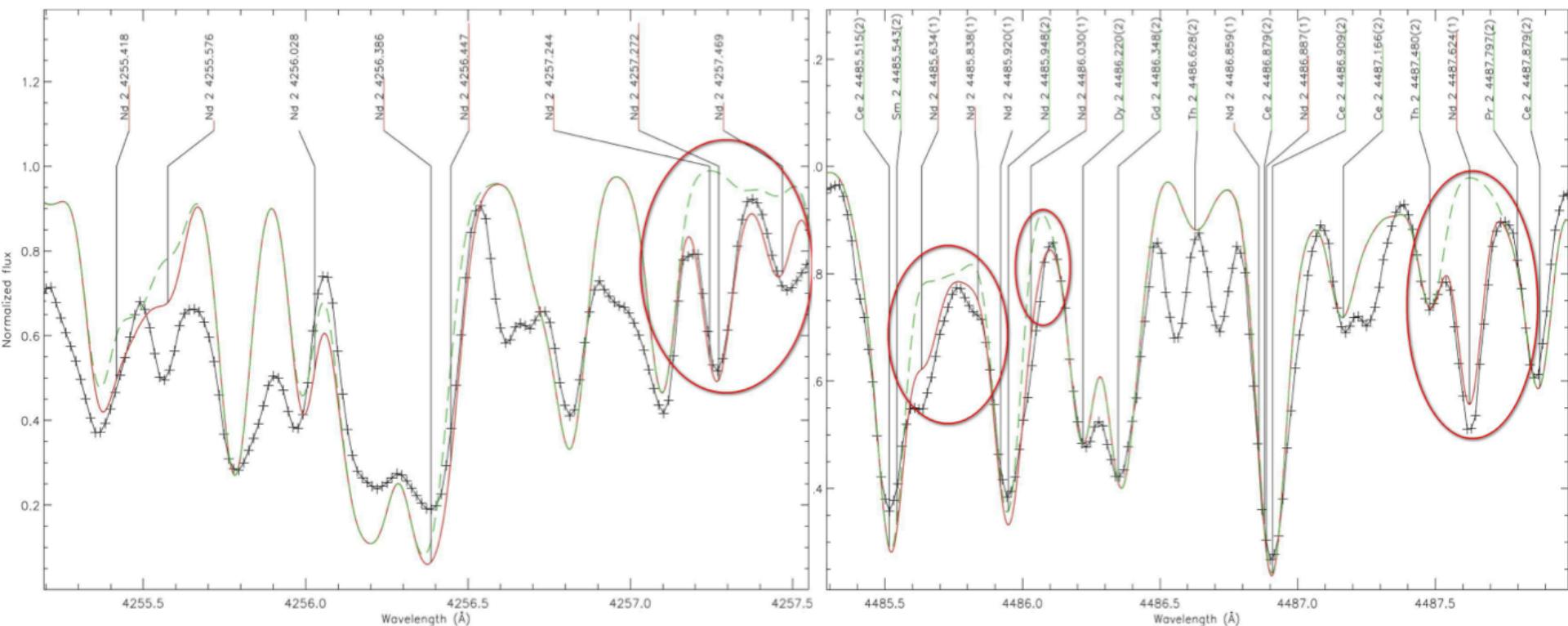
even $4f^25d$ + $4f^26d$ + $4f^26s$ + $4f^27s$ + $4f^28s$ + $4f5d6p$ + $4f6s6p$ + $4f5d5f$ + $5p^54f^35d$ + $5p^54f^36s$
Std= 59 and 56 cm⁻¹.

Application to the analysis of Pr abundance in the atmosphere of Am star 32 Aqr (Ryabchikova et al)

New analysis of Nd II spectrum for search of Nd II lines in the spectrum of Przybylski' star (HD 101065)

597 levels of the odd $4f^35d6s + 4f^35d^2 + 4f^36s^2 + 4f^46p + 5p^64f^5$
 configurations and 233 levels of the even $4f^46s + 4f45d + 4f^36s6p$
 $+ 4f^35d6p$ configurations interpreted with a STD of respectively
 87 and 57 cm^{-1}

In VALD 1287 lines \rightarrow 5700 lines



Summary

Work in progress :

- Compilation of systematic trends by isoelectronic or isoionic sequences in singly and doubly ionized lanthanides (Ln II, Ln III)
⇒ estimation of scaling factors and energy intervals
- Analyses of Eu IV and of iron group elements Mn (IV, V), Fe VI, Ni (VII) , W V
- Precision measurements ($\pm 0.001\text{-}0.002\text{\AA}$) of Fe IV, V and Ni V wavelengths for variation of fundamental constants
- Improvements in U II, Th II
- MIT in Fe X
- VUV spectrum of HD
- Data on line on molat.obspm.fr

Fe X : magnetic field induced transition (MIT)

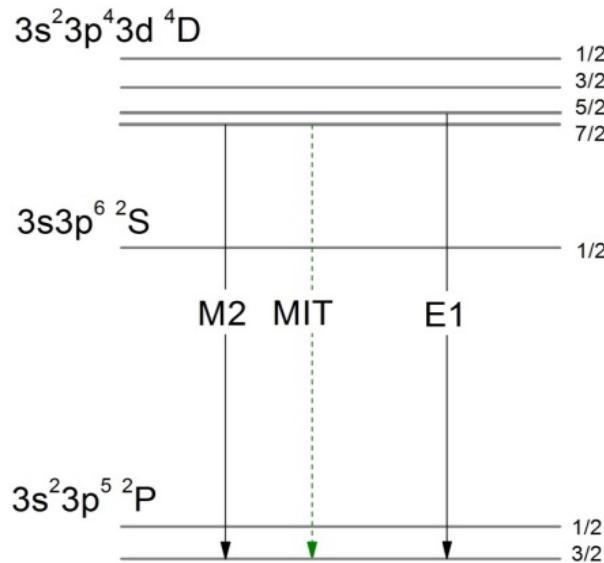


Figure 1: Schematic energy-level diagram for Chlorine-like ions with $Z < 26$ and zero nuclear spin, where ${}^4D_{7/2}$ is the lowest level in the configuration $3s^2 3p^4 4D$. For ions with $Z > 26$, a level crossing has occurred and ${}^4D_{5/2}$ is lower than ${}^4D_{7/2}$. Under the influence of an external magnetic field, an E1 transition opens up from the ${}^4D_{7/2}$ to the ground state through mixing with the ${}^4D_{5/2}$.

Newly identified lines and new experimental levels

molat.obspm.fr

(2007-2008)

-

Tm IV

- 760 lines, 209 energy levels

-

Nd IV

- 1426 lines, 232 levels

-

Eu III

- 90 new lines, 30 new levels
- (1150 Ritz wavelengths)

Nd V

- 160 lines 48 levels

-

More recent

-

Yb V (2013)

- 1080 lines, 242 energy levels

-

Nd V (2015) for core-excited configurations

- 304 lines, 104 energy levels

Er IV (2016)

- 591 lines, 120 energy levels

Thank you for your attention !